

Energy Markets III: Weather Derivates

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- **Stand-alone**

- temperature
- precipitation
- wind

- **In-Combination**

- natural gas
- power
- heating oil
- propane

- Agricultural risk (yield, revenue, input hedges and trading)
- Power outage - contingent power price options

For many contracts, delivery needs to match demand

- **Demand** for energy highly correlated with **temperature**
 - Heating Season (winter) HDD
 - Cooling Season (summer) CDD
- **Stylized Facts** and **First (naive) Models**
 - Electricity demand = $\beta * \text{weather} + \alpha$
 - Not true all the time
 - Time dependent β by filtering !
 - From the stack: Correlation (Gas,Power) = f(weather)
 - No significance, too unstable
 - Could it be because of heavy tails?
- **Weather dynamics** need to be included
 - **Another Source of Incompleteness**

- **Hedging Volume Risk**

- Protection against the Weather Exposure
- **Temperature Options** on CDDs (Extreme Load)

- **Hedging Basis Risk**

- Protection against Gas & Electricity Price Spikes
- Gas purchase with **Swing Options**

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- Use **Swing Options**
- Multiple Rights to deviate (within bounds) from base load contract level
- **Pricing & Hedging** quite involved!
 - Tree/Forest Based Methods
 - Direct Backward Dynamic Programming Induction (à la Detemple-Jaillet-Ronn-Tompaidis)
 - **New Monte Carlo Methods**
 - Nonparametric Regression (à la Longstaff-Schwarz) Backward Dynamic Programming Induction

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Review: **Classical Optimal Stopping Problem: American Option**

- $X_0, X_1, X_2, \dots, X_n, \dots$ rewards
- Right to ONE Exercise
- Mathematical Problem

$$\sup_{0 \leq \tau \leq T} \mathbb{E}\{X_\tau\}$$

Mathematical Solution

- Snell's Envelop
- Backward Dynamic Programming Induction in Markovian Case

Standard, Well Understood

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Standard, Well Understood

In its simplest form the problem of **Swing/Recall** option pricing is an

Optimal Multiple Stopping Problem

- $X_0, X_1, X_2, \dots, X_n, \dots$ rewards
- Right to N Exercises
- Mathematical Problem

$$\sup_{0 \leq \tau_1 < \tau_2 < \dots < \tau_N \leq T} \mathbb{E}\{X_{\tau_1} + X_{\tau_2} + \dots + X_{\tau_N}\}$$

- **Refraction** period θ

$$\tau_1 + \theta < \tau_2 < \tau_2 + \theta < \tau_3 < \dots < \tau_{N-1} + \theta < \tau_N$$

Part of recall contracts & crucial for continuous time models

- **Ubiquitous in Energy Sector**
 - Swing / Recall contracts
 - End user contracts (EDF)
- **Present in other contexts**
 - Fixed income markets (e.g. chooser swaps)
 - Executive option programs
 - Reload → Multiple exercise, Vesting → Refraction, ...
 - Fleet Purchase (airplanes, cars, ...)
- **Challenges**
 - Valuation
 - Optimal exercise policies
 - Hedging

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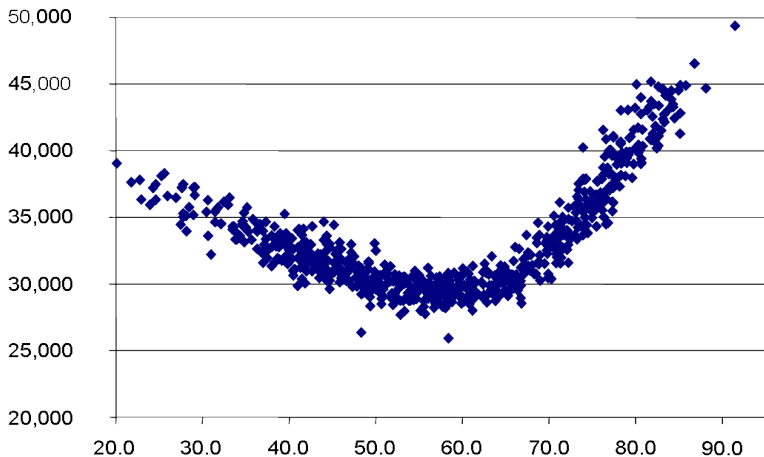
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Princeton University Electricity Budget

2.8 M \$ over (PU is small)

- The University has its own Power Plant
- Gas Turbine for Electricity & Steam
- Major Exposures
 - Hot Summer (air conditioning) Spikes in Demand, Gas & Electricity Prices
 - Cold Winter (heating) Spikes in Gas Prices

- Never Again such a Short Fall !!!
- Student (Greg Larkin) Thesis
- **Hedging Volume Risk**
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Average Daily Load against Average Daily Temperature (PJM data).

The Need for Temperature Options

- Rigorous Analysis of the Dependence between the Shortfall and the Temperature in Princeton
- Use of Historical Data (sparse) & Definition of a *Temperature Protection*
 - Period of the Coverage
 - Form of the Coverage
- Search for the Nearest Stations with HDD/CDD Trades
 - La Guardia Airport (LGA)
 - Philadelphia (PHL)
- Define a Portfolio of LGA & PHL forward / option Contracts
- Construct a LGA / PHL basket

Pricing: How Much is it Worth to PU?

- **Actuarial / Historical Approach**
 - Burn Analysis
 - Temperature Modeling & Monte Carlo VaR Computations
 - Not Enough Reliable Load Data
- **Expected (Exponential) Utility Maximization** (A. Danilova)
 - Use Gas & Power Contracts
 - Hedging in Incomplete Models
 - Indifference Pricing
 - Very Difficult Numerics (whether PDE's or Monte Carlo)

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OTC & Exchange traded (29 cities on CME)

- Still Extremely **Illiquid** Markets (except for **front month**)
- **Misconception**: Weather Derivative = Insurance Contract
 - No secondary market
 - Mark-to-Market (or Model) does not change
- Not Until Meteorology **kicks in** (10-15 days before maturity)
 - Mark-to-Market (or Model) **changes** every day
 - Contracts change hands
 - That's when major losses occur and money is made
- This **hot period** is not considered in academic studies
 - Need for **updates**: new information coming in (temperatures, forecasts,)
 - Filtering is (again) the solution

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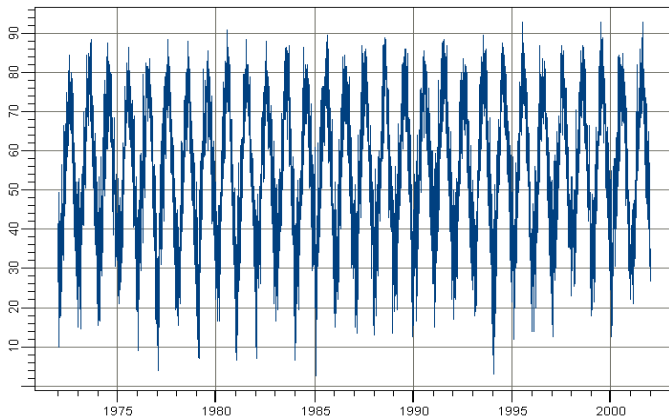
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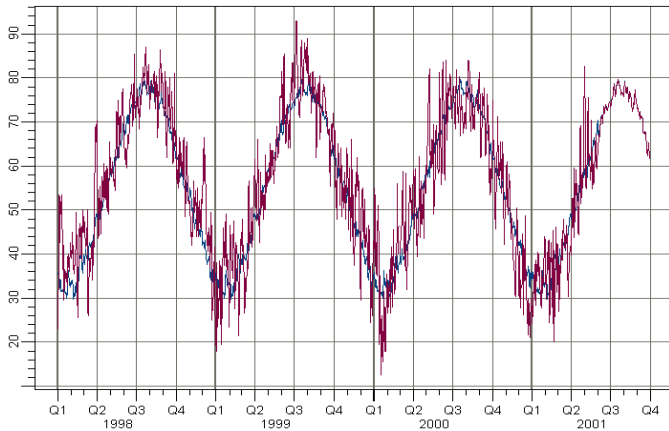
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La Guardia Daily Average Temperature



Daily Average Temperature at La Guardia.

Prediction on 6/1/2001 of Summer La Guardia Average Temperature



Prediction on 6/1/2001 of daily temperature over the next four months.

The Future of the Weather Markets

- **Social function** of the weather market
 - Existence of a Market of Professionals (for weather risk transfer)
- **Under attack** from
 - (Re-)Insurance industry
 - Utilities (trying to pass weather risk to end-customer)
 - EDF program in France
 - Weather Normalization Agreements in US
- **Cross Commodity Products**
 - Gas & Power contracts with **weather triggers/contingencies**
 - New (major) players: **Hedge Funds** provide liquidity
- **World Bank**
 - Use weather derivatives instead of insurance contracts

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Incomplete Market Model & Indifference Pricing

- Temperature Options: Actuarial/Statistical Approach
- Temperature Options: Diffusion Models (Danilova)
- Precipitation Options: Markov Models (Diko)
 - *Problem*: Pricing in an Incomplete Market
 - *Solution*: Indifference Pricing à la Davis

$$\begin{aligned}d\theta_t &= p(t, \theta)dt + q(t, \theta)dW_t^{(\theta)} + r(t, \theta)dQ_t^{(\theta)} \\dS_t &= S_t[\mu(t, \theta)dt + \sigma(t, \theta)dW_t^{(S)}]\end{aligned}$$

- θ_t **non-tradable**
- S_t **tradable**

Example: Exponential Utility Function

$$\tilde{p}_t = \frac{\mathbb{E}\{\tilde{\phi}(Y_T)e^{-\int_t^T V(s, Y_s)ds}\}}{\mathbb{E}\{e^{-\int_t^T V(s, Y_s)ds}\}}$$

where

- $\tilde{\phi} = e^{-\gamma(1-\rho^2)f}$
where $f(\theta_T)$ is the pay-off function of the European call on the temperature
- $\tilde{p}_t = e^{-\gamma(1-\rho^2)p_t}$
where p_t is price of the option at time t
- Y_t is the diffusion:

$$dY_t = \left[g(t, Y_t) - \frac{\mu(t, Y_t) - r}{\sigma(t, Y_t)} h(t, Y_t) \right] dt + h(t, Y_t) d\tilde{W}_t$$

starting from $Y_0 = y$

- V is the time dependent potential function:

$$V(t, y) = -\frac{1-\rho^2}{2} \frac{(\mu(t, y) - r)^2}{\sigma(t, y)^2}$$

The Weather Market Today

- Insurance companies: Swiss Re, XL, Munich Re, Ren Re
- Financial Houses: Goldman Sachs, Deutsche Bank, Merrill Lynch, ABN AMRO
- Hedge funds: D. E. Shaw, Tudor, Susquehanna, Centaurus, Wolverine

Trading

- OTC
- Exchange: CME (Chicago Mercantile Exchange) 29 cites globally traded, monthly / seasonal contracts
- Strong end-user demand within the energy sector Northeast and Midwest LDCs most prevalent in US

- Only a subset of locations are traded on a daily basis
- Exchange settlement prices depart from OTC market prices (viewed by traders)
- Denoting by μ the mean of the swaps delivering in a given season, by Σ their covariance matrix:

$$\inf_{\mu, \Gamma \mu = \pi} (\mu - \mu_{sim}^t \Sigma^{-1} (\mu - \mu_{sim}))$$

where Γ defines the set of observable trades and π is the vector of market prices.